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N22

Rounding to 1 Significant Figure

- 1) Round the following to 1 significant figure.
 - a) 478 cm
 - b) 450 cm
 - c) 449 cm
 - d) 12761 m
 - e) 28481 km
- 2) Round the following to 1 significant figure.
 - a) 673.8 cm
 - b) 4017.9 kg
 - c) 246.83 m
 - d) £45.38
 - e) 20482.1 kg
- 3) Round the following to 1 significant figure.
 - a) 0.26 ml
 - b) 0.043 g
 - c) 0.0671 m
 - d) 0.000256 km
 - e) 0.3822 m
- 4) Round the following to 1 significant figure.
 - a) 962 m
 - b) 0.923 cm
 - c) 0.971 cm
 - d) 0.096 km
 - e) 0.00985 km
- 5) Round the following to 1 significant figure.
 - a) £631428
 - b) 0.00573 g
 - c) £3614.68
 - d) 0.493 ml
 - e) £968

Level 7



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C26

Percentage Increase and Decrease

- 1) a) Increase £400 by 16%
 - b) Increase £750 by 24%
 - c) Increase £2000 by 38%
 - d) Increase £14500 by 19%
 - e) Increase £16.50 by 30%
- 2) a) Decrease £700 by 32%
 - b) Decrease £36 by 14%
 - c) Decrease £1970 by 40%
 - d) Decrease £3000 by 12.5%
 - e) Decrease £3124 by 16.25%
- 3) A sports shop reduces the price of all its trainers by 15% in the Spring sale. Before the sale, one pair of trainers cost £74. How much are they after the reduction?
- 4) Tim took up weightlifting.
 In his first session he could bench-press 45 kg.
 Four weeks later he could bench-press 22% more.
 How much could he now lift to the nearest kg?
- 5) If a manager of a shop reduces the price of a £1500 piano by 15% and then, four weeks later, increases the reduced price by 15%, how much does it now cost?

Level 7

N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 A26 A27 A28 A29 S30 S31 S32 S33 S34 S35 S36 S37 D14 D15

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Addition and Subtraction of Fractions

a)
$$\frac{1}{3} + \frac{1}{2}$$

b)
$$\frac{3}{5} + \frac{1}{4}$$

c)
$$\frac{2}{7} + \frac{3}{5}$$

d)
$$\frac{1}{2} + \frac{2}{9}$$

e)
$$\frac{3}{10} + \frac{3}{7}$$

a)
$$1\frac{2}{3} + \frac{3}{4}$$

b)
$$2\frac{1}{2} + \frac{5}{7}$$

c)
$$\frac{2}{5} + 3\frac{1}{2}$$

d)
$$1\frac{7}{10} + \frac{1}{5}$$

e)
$$2\frac{3}{4} + \frac{5}{6}$$

a)
$$\frac{2}{3} - \frac{1}{2}$$

b)
$$\frac{3}{4} - \frac{2}{3}$$

c)
$$\frac{4}{5} - \frac{3}{4}$$

d)
$$\frac{5}{6} - \frac{2}{3}$$

e)
$$\frac{3}{4} - \frac{3}{8}$$

a)
$$4\frac{1}{2} - 2\frac{1}{2}$$

b)
$$1\frac{2}{5} - 1\frac{1}{10}$$

c)
$$3\frac{2}{3} - 1\frac{11}{15}$$

d)
$$2\frac{3}{4} - 1\frac{5}{8}$$

e)
$$5\frac{2}{3} - 1\frac{4}{9}$$

Work out 2)

a)
$$\frac{2}{3} + \frac{1}{6}$$

b)
$$\frac{3}{5} + \frac{3}{10}$$

c)
$$\frac{1}{2} + \frac{4}{5}$$

d)
$$\frac{5}{6} + \frac{3}{5}$$

e)
$$\frac{7}{12} + \frac{3}{4}$$

4) Work out

a)
$$2\frac{1}{2} + 1\frac{1}{5}$$

b)
$$1\frac{3}{4} + 1\frac{2}{3}$$

c)
$$3\frac{1}{6} + 1\frac{1}{3}$$

d)
$$2\frac{2}{9} + 1\frac{2}{3}$$

e)
$$4\frac{1}{2} + 2\frac{3}{10}$$

6) Work out

a)
$$1\frac{3}{4} - \frac{1}{2}$$

b)
$$2\frac{4}{5} - \frac{3}{4}$$

c)
$$3\frac{1}{6} - \frac{2}{3}$$

d)
$$2\frac{2}{9} - \frac{5}{6}$$

e)
$$6\frac{1}{2} - \frac{7}{8}$$

8) Work out

a)
$$3\frac{4}{5} + 1\frac{1}{2}$$

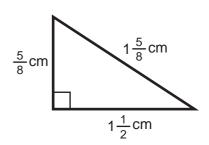
b)
$$4\frac{2}{9} - \frac{5}{6}$$

c)
$$2\frac{3}{8} + 1\frac{5}{6}$$

d)
$$2 - 1\frac{5}{8}$$

e)
$$5-2\frac{1}{7}$$

- 9) Find the perimeter of the rectangle below. Give your answer as a mixed number.
- $3\frac{1}{3}$ cm $2\frac{3}{4}$ cm
- 10) Find the perimeter of the triangle below. Give your answer as a mixed number.



If a length of copper tubing is $20\frac{1}{4}$ cm long and Jim cuts off a piece that is $17\frac{3}{5}$ cm long, what is the length of the copper tubing left over?



Multiplication and Division of Fractions

a)
$$\frac{1}{2} \times \frac{3}{4}$$

b)
$$\frac{2}{3} \times \frac{4}{5}$$

c)
$$\frac{10}{11} \times \frac{2}{3}$$

d)
$$\frac{4}{9} \times \frac{2}{5}$$

e)
$$\frac{4}{7} \times \frac{1}{9}$$

a)
$$1\frac{1}{2} \times \frac{8}{9}$$

b)
$$2\frac{2}{3} \times \frac{6}{7}$$

c)
$$\frac{6}{11} \times 1\frac{1}{8}$$

d)
$$4\frac{2}{5} \times \frac{10}{11}$$

e)
$$3\frac{3}{4} \times \frac{8}{9}$$

a)
$$\frac{2}{3} \div \frac{1}{2}$$

b)
$$\frac{3}{4} \div \frac{2}{3}$$

c)
$$\frac{2}{5} \div \frac{3}{4}$$

d)
$$\frac{3}{7} \div \frac{6}{11}$$

e)
$$\frac{3}{4} \div \frac{3}{8}$$

a)
$$2\frac{1}{2} \div 3\frac{1}{2}$$

b)
$$3\frac{2}{5} \div 1\frac{1}{10}$$

c)
$$4\frac{1}{3} \div 1\frac{11}{15}$$

d)
$$2\frac{3}{4} \div 1\frac{5}{8}$$

e)
$$5\frac{2}{3} \div 1\frac{4}{9}$$

Work out 2)

a)
$$\frac{2}{3} \times \frac{3}{5}$$

b)
$$\frac{3}{7} \times \frac{5}{6}$$

c)
$$\frac{8}{9} \times \frac{6}{10}$$

d)
$$\frac{1}{2} \times \frac{8}{9}$$

e)
$$\frac{7}{10} \times \frac{5}{21}$$

4) Work out

a)
$$2\frac{1}{2} \times 2\frac{1}{5}$$

b)
$$3\frac{3}{4} \times 2\frac{2}{3}$$

c)
$$4\frac{1}{6} \times 2\frac{2}{5}$$

d)
$$2\frac{2}{9} \times 1\frac{1}{5}$$

e)
$$3\frac{4}{7} \times 1\frac{13}{15}$$

6) Work out

a)
$$\frac{3}{4} \div 1\frac{1}{5}$$

b)
$$\frac{4}{7} \div 1\frac{7}{9}$$

c)
$$2\frac{1}{4} \div \frac{6}{7}$$

d)
$$2\frac{3}{5} \div \frac{9}{10}$$

e)
$$1\frac{1}{2} \div \frac{3}{8}$$

8) Work out

a)
$$\frac{2}{3} \div 2$$

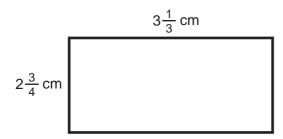
b)
$$1\frac{3}{4} \div 14$$

c)
$$4 \div \frac{2}{5}$$

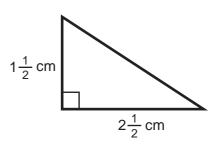
d)
$$5 \div \frac{3}{4}$$

e)
$$3\frac{1}{2} \div 4$$

Find the area of the rectangle below. 9) Give your answer as a mixed number.



10) Find the area of the triangle below. Give your answer as a mixed number.



Jim has a length of copper tubing which is 85 cm long. 11) He wants to cut it into pieces which are $4\frac{1}{4}$ cm long. If there is no wastage, how many pieces will Jim get?

- C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 S30 S31 S32 S33 S34 S35 S36 S37 D14 D15

Numbers Between 0 and 1 (Multiplication and Division)

- 1) Work out the answers to the following:
 - a) 24×0.2
 - b) 13×0.4
 - c) 60×0.7
 - d) 243×0.2
 - e) 0.6×700
- 2) Work out the answers to the following:
 - a) 314×0.02
 - b) 836×0.001
 - c) 800×0.006
 - d) 418×0.003
 - e) 411×0.09
- 3) Work out the answers to the following:
 - a) 0.2×0.4
 - b) 0.1×0.03
 - c) 0.02×0.06
 - d) 0.08×0.003
 - e) 0.05×0.08
- 4) Work out the answers to the following:
 - a) 62×0.14
 - b) 2.7×2.5
 - c) 613×0.042
 - d) 42.3×1.8
 - e) 228 x 0.063

- 5) Work out the answers to the following:
 - a) $6 \div 0.2$
 - b) $8 \div 0.1$
 - c) $9 \div 0.3$
 - d) $4 \div 0.02$
 - e) $7 \div 0.002$
- 6) Work out the answers to the following:
 - a) $62 \div 0.2$
 - b) $51 \div 0.3$
 - c) $4.56 \div 0.04$
 - d) $22.5 \div 0.05$
 - e) $14.7 \div 0.007$
- 7) Work out the answers to the following:
 - a) $7.24 \div 0.2$
 - b) $8.13 \div 0.3$
 - c) $1.512 \div 0.07$
 - d) $0.16 \div 0.008$
 - e) $0.0732 \div 0.04$
- 8) Work out the answers to the following:
 - a) $0.718 \div 0.2$
 - b) $0.0141 \div 0.003$
 - c) $0.24 \div 0.012$
 - d) $1.625 \div 0.0013$
 - e) 47.1 ÷ 0.15

C30

Estimating Answers

- 1) Estimate the value of:
 - a) 21×34
 - b) 42×56
 - c) 17×62
 - d) 29×78
 - e) 66×96
- 2) Estimate the value of:
 - a) 510×724
 - b) 86 × 2146
 - c) 753×184
 - d) 48×6315
 - e) 3642 x 1356
- 3) Estimate the value of:
 - a) $\frac{61}{19}$
 - b) $\frac{76}{43}$
 - c) $\frac{362}{78}$
 - d) $\frac{738}{96}$
 - e) $\frac{416}{781}$

- 4) Estimate the value of:
 - a) $\frac{357}{12 \times 23}$
 - b) $\frac{924}{34 \times 13}$
 - c) $\frac{172 \times 411}{430}$
 - d) $\frac{625 \times 43}{16 \times 38}$
 - e) $\frac{972 \times 368}{17 \times 23 \times 18}$
- 5) Estimate the value of:
 - a) $8 \div 0.12$
 - b) $6 \div 0.24$
 - c) $5 \div 0.49$
 - d) $7 \div 0.012$
 - e) $23 \div 0.18$
- 6) Estimate the value of:
 - a) $\frac{24 \times 510}{0.53}$
 - b) $\frac{46 \times 6.2}{0.135}$
 - c) $\frac{215 \times 38}{0.183}$
 - d) $\frac{18.3 \times 31.2}{0.017}$
 - e) $\frac{405 \times 274}{0.488}$

- 1) Using a calculator, work out the value of:
 - a) $24 + 16 \div 4$
 - b) $3 + 8 \div 2 \times 3$
 - c) $60 \times 2 20 \div 4$
 - d) $(2 + 7 \times 8) \times 4$
 - e) $(3+7) \times (8-2)$
- Using a calculator, work out the value of: 2)
 - a) $6^3 (2^4 + 3^5)$
 - b) $(3^7 2^6) \div 10^4$
 - c) $2^8 \div 2^3 \times 5^2$
 - d) $5^3 \times 3^5$
 - e) $2^{20} 3^8$
- 3) Using a calculator, work out the value of:
 - a) $\sqrt{256} \times 2^4 \sqrt{169}$
 - b) $\sqrt{365} \times \sqrt{365}$
 - c) $\sqrt{550-21}$
 - d) $\sqrt{2^8 + 3^4 13}$
 - e) $\sqrt{4^6 \times 2^8} \div (3^2 1)$
- 4) Using a calculator, work out the value of:
 - a) $\frac{7+4\times8}{18-5}$
- d) $\frac{62 \times 2^4 + 2^3}{\sqrt{4^3 + 3^2 + 3^3}}$
- b) $\frac{6^3 2^3}{(3^2 + 7) \div 2}$ e) $\frac{284 \sqrt{2^9 112}}{(3 + 17) \times \sqrt{100}}$
- c) $\frac{\sqrt{729} + 21}{\sqrt{64}}$

Level 7

Further Algebraic Simplification

- 1) Simplify the following
 - a) $6 \times x$
 - b) $2 \times x \times y$
 - c) $6 \times x \times 3 \times y$
 - d) $s \times t \times u$
 - e) $7 \times s \times 2 \times t \times u$
- 2) Simplify the following
 - a) $x \times x \times x \times x$
 - b) $t \times t \times t \times t \times t \times t \times t$
 - c) $g \times g$
 - d) $x \times x \times x \times y \times y \times y \times y$
 - e) $x \times y \times x \times y \times y$
- 3) Simplify the following
 - a) $x \times x^2$
 - b) $y^3 \times y^4$
 - c) $X^2 \times X^3 \times X$
 - d) $g \times g \times g^2 \times g^4$
 - e) $X^2 \times X^3 \times X^4 \times X^5$
- 4) Simplify the following
 - a) $3x^2 \times 2x^3$
 - b) $5x \times 4x^2$
 - c) $6y^3 \times 2y^4$
 - d) $9x^2 \times x^3$
 - e) $4x^3 \times 2x \times 3x^2$
- 5) Simplify the following
 - a) $3x^2y^3 \times 2x^3y^4$
 - b) $2xy^4 \times 3x^2y$
 - c) $5x^3y^4 \times 2x^2y^2$
 - d) $2x^2y \times x^4y^2$
 - e) $3x^3y \times 2xy^2 \times 3x^2y^2$

6) Simplify the following

- a) $x^8 \div x^2$
- b) $9y^6 \div 3y^2$
- c) $14y^3 \div 2y^2$
- d) $20x^5 \div 4x$
- e) $16x^8 \div 8x^2$

7) Simplify the following

- a) $\frac{12x^6}{3x^2}$
- b) $\frac{20x^3}{2x}$
- c) $\frac{5x^4}{x^2}$
- d) $\frac{6x^5}{3x^3}$
- e) $\frac{300x^9}{10x^2}$

8) Simplify the following

- a) $\frac{12x^3y}{4x}$
- b) $\frac{15x^4y^2}{3xy}$
- c) $\frac{20x^3y^6}{4x^2y^3}$
- $d) \quad \frac{14x^2y^2}{7xy}$
- e) $\frac{30x^2y^3z^6}{3xy^2z^4}$

9) Find the value of

- a) 4º
- b) 6°
- c) 12⁰
- d) z^0
- e) x^0

Expanding Brackets

A17

- 1) Expand
 - a) 2(x + 3)
 - b) 2(x-4)
 - c) 5(2x + 1)
 - d) 7(3x-1)
 - e) 4(2a + 7)
- 2) Expand
 - a) 2x(3x + 1)
 - b) 3x(4x-2)
 - c) 2x(x + 1)
 - d) 3x(2x-y)
 - e) 5x(3x + 2y)
- 3) Expand and simplify
 - a) 2(x+3) + 4(x+1)
 - b) 3(2x+1)+2(5x+2)
 - c) 4(x+1) + 3(3x+4)
 - d) 6(2x+3)+5(x+2)
 - e) 4(3x + 2) + 5(2x + 1)
- 4) Expand and simplify
 - a) 2(5x+3)+3(x-1)
 - b) 3(4x+5)+2(3x-4)
 - c) 5(2x-1)+3(2x+5)
 - d) 2(3x-4)+3(x+2)
 - e) 3(2x-1)+4(3x-2)
- 5) Expand and simplify
 - a) 3(x+2)-2(x+3)
 - b) 4(2x+3)-3(2x+1)
 - c) 5(3x-2)-2(x-2)
 - d) 2(5x-1)-4(2x-3)
 - e) 3(2x+7)-2(3x+2)

- 6) Expand and simplify
 - a) (x+2)(x+2)
 - b) (x+3)(x+5)
 - c) (x+7)(x+1)
 - d) (x + 4)(x + 3)
 - e) (x + 7)(x + 2)
- 7) Expand and simplify
 - a) (2x+1)(3x+2)
 - b) (4x + 3)(2x + 1)
 - c) (3x + 4)(3x + 2)
 - d) (5x + 2)(5x + 7)
 - e) (2x + 10)(2x + 4)
- 8) Expand and simplify
 - a) (x+5)(x-3)
 - b) (x-2)(x+4)
 - c) (x-6)(x-2)
 - d) (x+7)(x+3)
 - e) (x-8)(x-2)
- 9) Expand and simplify
 - a) (2x-1)(3x+4)
 - b) (5x-2)(3x-1)
 - c) (3x+4)(2x-3)
 - d) (5x-1)(5x-2)
 - e) (4x + 2)(3x 5)
- 10) Expand and simplify
 - a) $(x + 5)^2$
 - b) $(x-2)^2$
 - c) $(2x + 3)^2$
 - d) $(3x-1)^2$
 - e) $(4x + 3)^2$

Factorisation

A18

- 1) Factorise the following
 - a) 6x 2
 - b) 8x + 14
 - c) 6x + 9
 - d) 10x 5
 - e) 12x + 18
- 2) Factorise the following
 - a) $x^2 + x$
 - b) $t^2 t$
 - c) $x^3 + x$
 - d) $x^5 x^2$
 - e) $a^7 + a^4$
- 3) Factorise the following
 - a) $3x^2 + 6x$
 - b) $8x^3 2x$
 - c) $12a^2 + 4a^3$
 - d) $20x^4 6x^2$
 - e) $7x^3 + 8x$

- 4) Factorise the following
 - a) $6x^2y^4 + 4xy^3$
 - b) $4x^3y^4 + 2x^2y^2$
 - c) $10x^4y^3z 5xy^5z$
 - d) $16a^2b^3c^4 + 3ab^2c^3$
 - e) $9x^2y^4z 6xy^2z$
- 5) Factorise the following
 - a) 10x + 4
 - b) $X^4 X^2$
 - c) $9x^5 12x^2$
 - d) $12x^2y^3 + 4xy^2$
 - e) $24x^3yz^4 10xz^2$

Solving Difficult Equations

A19

1) Solve the following

a)
$$2x + 3 = 19$$

b)
$$3x - 2 = 13$$

c)
$$5x - 1 = 9$$

d)
$$3 + 2x = 23$$

e)
$$12 - 3x = 9$$

2) Solve the following

a)
$$2(3x-1)=22$$

b)
$$3(x+7) = 18$$

c)
$$4(5x-2) = 12$$

d)
$$66 = 6(2x + 3)$$

e)
$$20 = 5(x - 6)$$

3) Solve the following

a)
$$\frac{x-6}{2} = 3$$

b)
$$\frac{x+8}{3} = 5$$

c)
$$\frac{2x-1}{3} = 5$$

d)
$$\frac{6x+1}{2} = 8$$

e)
$$\frac{7x-3}{5} = 5$$

4) Solve the following

a)
$$2x + 7 = x + 12$$

b)
$$4x - 5 = 2x + 3$$

c)
$$7x + 2 = 3x + 26$$

d)
$$6x - 7 = 4x - 5$$

e)
$$3x + 4 = x - 7$$

5) Solve the following

a)
$$x-6=2x-13$$

b)
$$3x + 4 = 5x - 8$$

c)
$$4x + 17 = x - 4$$

d)
$$5-2x=x-7$$

e)
$$2x - 1 = 14 - 3x$$

6) Solve the following

a)
$$2(3x-1) = 4x + 7$$

b)
$$3(x+4) = 2(x-5)$$

c)
$$5(2x-3) = 3(3x+4)$$

d)
$$2(2x-1) = 5(2x-4)$$

e)
$$2(2x+3) = 5(x+3)$$

7) Solve the following

a)
$$\frac{2(x+1)}{3} = 6$$

b)
$$\frac{4(2x-3)}{5} = 4$$

c)
$$\frac{2(4x-5)}{3} = x + 10$$

d)
$$\frac{3(5x+4)}{2} = 7x - 8$$

e)
$$4-x=\frac{2(x+7)}{3}$$

Rearranging a Formula

A20

- 1) Rearrange to make *x* the subject of the formula
 - a) y = x 2
 - b) y = x + 7
 - c) y = x + t
 - d) y = 5x + 3
 - e) y = 2x 4
- 2) Rearrange to make *x* the subject of the formula
 - a) 3x + 2 = y
 - b) 4x 1 = y
 - c) ax 3 = y
 - d) ax + m = t
 - e) x + y = t
- 3) Rearrange to make *x* the subject of the formula
 - a) y = x + t v
 - b) ax c = y
 - c) y = ax tv + c
 - d) y + x = ct
 - e) c + ax + t = y + m
- 4) Rearrange to make *x* the subject of the formula
 - a) $\frac{x+2}{3} = y$
 - b) $y = \frac{x-4}{5}$
 - c) $\frac{5x-2}{4} = y$
 - d) $\frac{ax+c}{m} = y$
 - e) $k = \frac{t + mx}{y}$

- 5) Rearrange to make *x* the subject of the formula
 - a) $y = \frac{3x}{4}$
 - b) $y = \frac{2x}{5} 8$
 - c) $y = \frac{CX}{t} + m$
 - d) y = abx + c
 - e) $\frac{mx}{t} + c = y$
- 6) Rearrange to make *x* the subject of the formula
 - a) y = 4(x + t)
 - b) y = a(x m)
 - c) at(c + x) = y
 - d) y + m = a(c + x)
 - e) t v = m(x y)
- 7) Rearrange to make *x* the subject of the formula
 - a) $\frac{x-u}{4} = y$
 - b) $\frac{x+a}{b} = c$
 - c) $\frac{3(x+2)}{c} = y$
 - d) $\frac{a(x+b)}{c} = d$
 - e) $\frac{t(x+c)}{d} = e + f$

Trial and Improvement

A21

The equation x² + 3x = 37
has a solution between 4 and 5.
 Use a trial and improvement method to find this solution.
Give your answer to one decimal place.
You must show ALL your working.

The equation x² - 4x = 6
 has a solution between 5 and 6.
 Use a trial and improvement method to find this solution.
 Give your answer to one decimal place.
 You must show ALL your working.

Level 7

N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 A26 A27 A28 A29 S30 S31 S32 S33 S34 S35 S36 S37 D14 D15

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Trial and Improvement

A21

The equation x³ + 3x = 114
 has a solution between 4 and 5.
 Use a trial and improvement method to find this solution.
 Give your answer to one decimal place.
 You must show ALL your working.

The equation x³ - 2x = 9
 has a solution between 2 and 3.
 Use a trial and improvement method to find this solution.
 Give your answer to one decimal place.
 You must show ALL your working.

Level 7

N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 A26 A27 A28 A29 S30 S31 S32 S33 S34 S35 S36 S37 D14 D15

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Inequalities

3)

If x is an integer, what are the

possible values of x?

 $-4 \le x \le 2$

 $-3 \le x < 1$

 $1 < x \le 5$

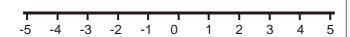
 $-3 < x \le 4$

 $-7 \le x \le -4$

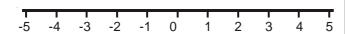
c)

A22

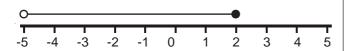
- 1) Represent the inequalities on the number lines.
 - a) $x \le 3$



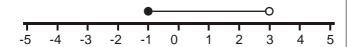
b) $-1 < x \le 4$



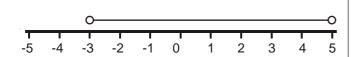
- c) $-3 \le x \le 3$
- -5 -4 -3 -2 -1 0 1 2 3 4 5
- 2) Write down the inequalities shown below
 - a)



b)



c)



Level 7

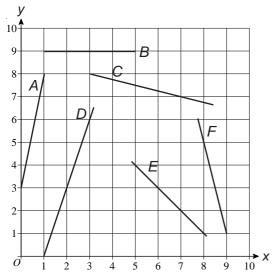
Solving Inequalities

A23

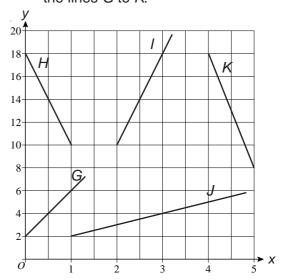
- 1) Solve
 - a) $2x 1 \ge 7$
 - b) 3x + 4 < 19
 - c) $5x 7 \le 18$
 - d) 2x + 9 > 5
 - e) $4x + 11 \le 14$
- 2) Solve
 - a) $\frac{x}{3} < 7$
 - b) $\frac{X}{5} 1 \ge 3$
 - c) $\frac{2x}{3} + 4 \le 9$
 - d) $12 \ge 2x 1$
 - e) 20 < 5 + 5x
- 3) Solve
 - a) $2(5x-1) \le 18$
 - b) 3(4x + 2) > 60
 - c) 42 > 2(6x + 15)
 - d) $4(1 + x) \le 12$
 - e) 8(2x-1) > 12
- 4) Solve
 - a) $2x + 7 \le x + 9$
 - b) x-6 > 3x-18
 - c) 4x + 3 < 2x 9
 - d) $2x 4 \ge 7x 34$
 - e) 2(x+3) < x-1

Understanding Straight Line Graphs

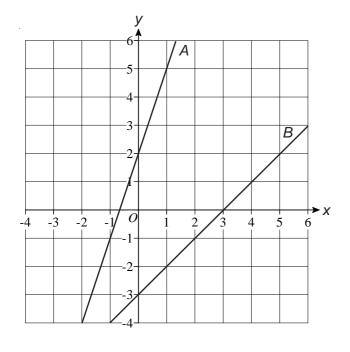
1) Find the gradients of the lines *A* to *F*.



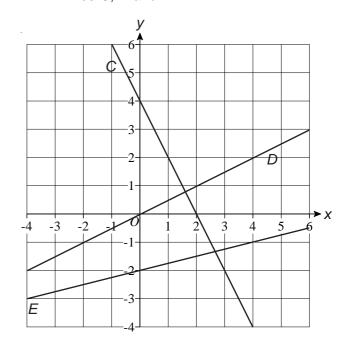
2) Find the gradients of the lines *G* to *K*.



3) Find the equations of lines *A* and *B*.



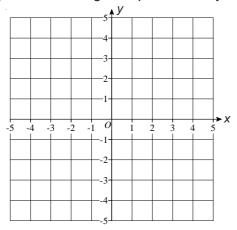
4) Find the equations of lines *C*, *D* and *E*.



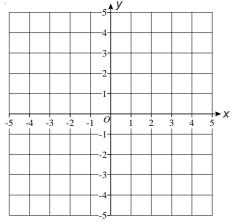
Level 7

Regions

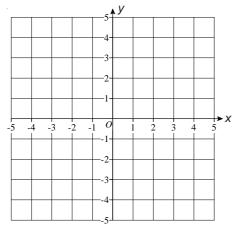
- 1) a) Shade the region represented by $x \le -1$
 - b) Shade the region represented by x > 3



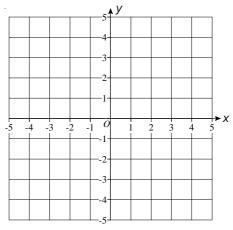
- 2) a) Shade the region represented by y < -1
 - b) Shade the region represented by $y \ge 2$



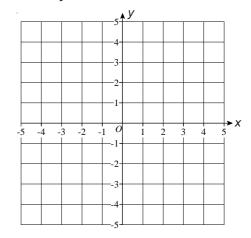
3) Shade the region represented by $-3 \le x < 2$



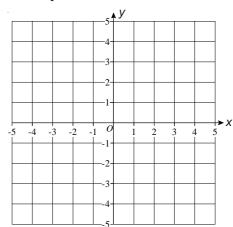
4) Shade the region represented by $1 \le y \le 4$



5) Shade the region where $-1 \le x \le 3$ and $-4 \le y \le -2$



6) Shade the region where -3 < x < 2and -1 < y < 4



Simultaneous Equations Graphically

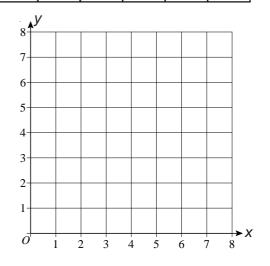
1) a) Complete the table of values for y = x + 2

b)	١	Drow	tho	aranh	٥f	· / –	v 1	2
D,)	Diaw	uie	graph	OI	y =	ΧŤ	_

- c) Complete the table of values for x + y = 7
- d) Draw the graph of x + y = 7
- e) Use your graph to solve the simultaneous equations y = x + 2 and x + y = 7

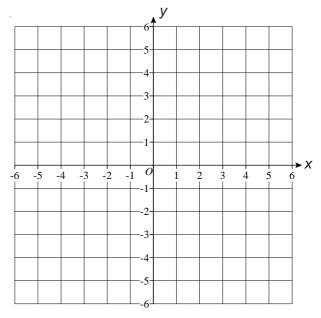
Х	0	1	2	3	4
У					

Х	0	1	2	3	4
У					



2) Using a graphical method, solve the simultaneous equations

$$y = 2x - 3$$
 and $y = 6 - x$



- 3) Solve the simultaneous equations y = x + 6 and y = 3 x
- 4) Solve the simultaneous equations y = x 14 and y = 2 3x

Level 7

Simultaneous Equations Algebraically

1)	Solve	3x + y = 11 $4x - y = 3$
2)	Solve	2x - 5y = 3 $4x + 5y = 21$
3)	Solve	x - 2y = 3 $3x + 2y = 5$
4)	Solve	x + 3y = 10 $x + y = 6$
5)	Solve	3x + 2y = 3 $2x + 2y = 5$
6)	Solve	5x - 3y = 23 $2x - 3y = 11$
7)	Solve	3x - 2y = 6 $x + y = 7$
8)	Solve	6x + y = 10 $2x - 3y = 10$
9)	Solve	2x + 7y = 11 $3x - 2y = 4$
10)	Solve	4x + 3y = 9 $5x + 2y = 13$
11)	Solve	2x + 3y = -7 $7x - 2y = -12$
12)	Solve	3x - 2y = 5 $9x + 5y = -7$

- 13) In the first week of opening, a zoo sold 200 adult tickets and 300 child tickets. The takings for that week were £2600. In the second week, 500 adult tickets were sold and 400 child tickets were sold. The takings for the second week were £5100. Form two equations and solve them to find the price of an adult ticket and the price of a child ticket.
- If you multiply Sid's age by four and Tony's age by five and add the answers together it comes to 259 years.
 However, if you multiply Sid's age by seven and then take away two times Tony's age the answer is 120 years.
 Form two equations and solve them to find the ages of Sid and Tony.
- 15) If nine rats and seven ferrets cost £116.75 and four rats and six ferrets cost £88, how much would five rats and four ferrets cost?
- 16) If a mouse and a goldfish cost £1.10 and the mouse costs £1 more than the goldfish, how much does the goldfish cost?

Level 7

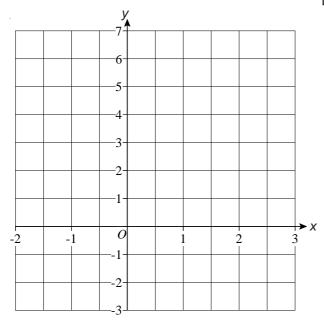
nth Term of Quadratic Sequences

- 1) Find the *n*th term of
 - a) 1, 4, 9, 16, 25,
 - b) 2, 5, 10, 17, 26,
 - c) 0, 3, 8, 15, 24,
- 2) Find the *n*th term of
 - a) 1, 4, 9, 16, 25,
 - b) 2, 8, 18, 32, 50,
 - c) 0.5, 2, 4.5, 8, 12.5,
- 3) Find the *n*th term of
 - a) 3, 9, 19, 33, 51,
 - b) 1, 7, 17, 31, 49,
 - c) 11, 41, 91, 161, 251,
- 4) For the following *n*th terms, find the first three terms and the tenth term
 - a) $n^2 + 4$
 - b) $n^2 3$
 - c) $n^2 + 10$
 - d) $n^2 + 2n$
 - e) $n^2 n$
- 5) For the following *n*th terms, find the first three terms and the tenth term
 - a) $4n^2$
 - b) $2n^2 + 3n$
 - c) $3n^2 2n$
 - d) $n^2 + n + 1$
 - e) $2n^2 + 4n 3$

Graphs of Quadratic and Cubic Functions

- 1) a) Complete the table of values for $y = x^2 2$
 - b) Draw the graph of $y = x^2 2$

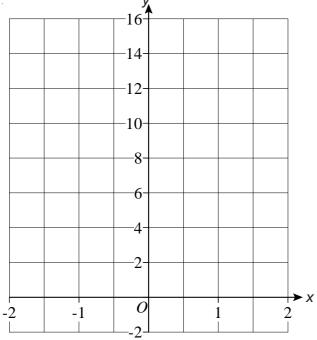
Х	-2	-1	0	1	2	3
У		-1			2	



c) Use the graph to estimate the values of x when y = 1

- 2) a) Complete the table of values for $y = 4x^2$
 - b) Draw the graph of $y = 4x^2$

X	-2	-1	0	1	2
У		4			16



c) Use the graph to estimate the value of y when x = 1.5

Level 7

Graphs of Quadratic and Cubic Functions

- 1) a) Complete the table of values for $y = x^2 + 2x$
 - b) Draw the graph of $y = x^2 + 2x$

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		-14-						
		14						
		-13-						
		-12-						
		-12-						
		-11-						
		10						
		-10-						
-		9-						
		8-						
		0-						
		 7-						
		6-						
		5-						
		4						
		-4-						
		3-						
		_						
		2-						
		1-						-
-2	-1	0		1	- 1	2	3	> X
		1-						J

Х	-2	-1	0	1	2	3
У		-1			8	

c) Use the graph to estimate the values of x when y = -0.5

- 2) a) Complete the table of values for $y = x^2 2x + 1$
 - b) Draw the graph of $y = x^2 2x + 1$

		y			
		12			
		-11			
		-10			
		9			
		8			
		 7			
		6			
		5			
		4			
		3			
		2			
		1-1-			
2	-1	0	1	2	3

Х	-2	-1	0	1	2	3
У		4			1	

c) Use the graph to estimate the value of y when x = 2.5

Level 7

Graphs of Quadratic and Cubic Functions

У

1) a) Complete the table of values for $y = 2x^2 + 2x - 3$

b) Diaw the graph of y = 2x + 2x 3	b)	Draw the graph of $y = 2x^2 + 2x - 3$
------------------------------------	----	---------------------------------------

Х	-2	-1	0	1	2
У		-3			9

- c) Use the graph to estimate the values of x when y = -2

-2

10

2) a) Complete the table of values for $y = x^3 + x$

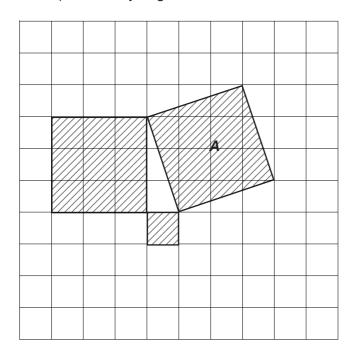
b) Draw the graph of $y = x^3 + x$

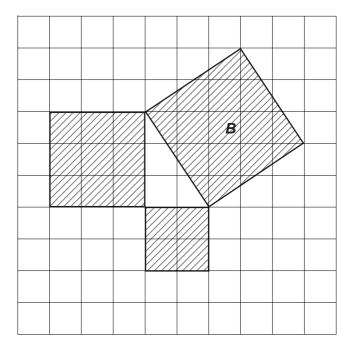
		1	10 ^				
			10				
			-8+				
			-6				
			-4+				-
			-2+				
			_				
-2	-1		0]	l	2	→ <i>x</i> 2
-2	-1		<i>O</i> -2-]	L	2	→ x 2
-2	-1		- 1]			2 2
-2	-1		-2]			2 2
-2	-1		-2+ -4+ -6+	1		,	x 2
-2	-1		-2 -4 	1			2 2

Level	7

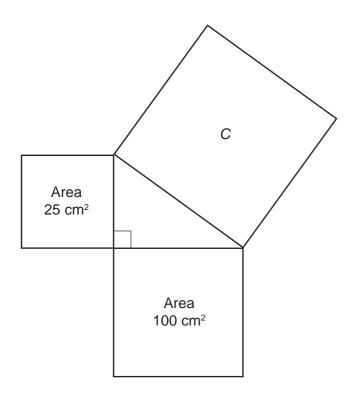
Pythagoras' Theorem

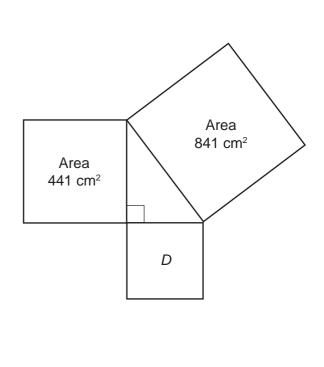
1) Use Pythagoras' theorem to work out the areas of squares A and B.





2) Use Pythagoras' theorem to work out the areas of squares C and D.





Level 7

S30 Pythagoras' Theorem

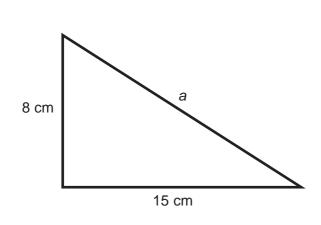
1) Find the lengths of the sides of these three squares.

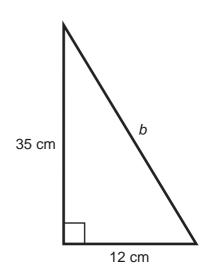
Area 529 cm²

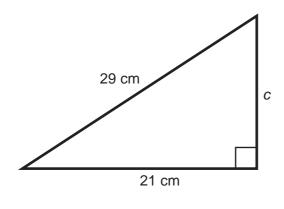
Area 210.25 cm²

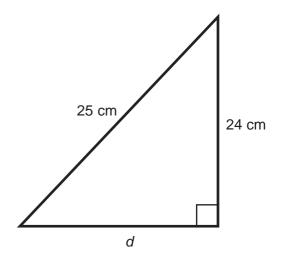
Area 152.7696 cm²

2) Find the lengths of the sides labelled a to d.





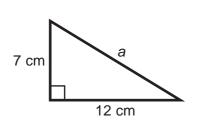


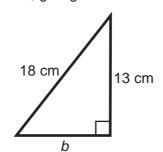


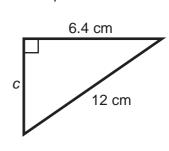
Level 7

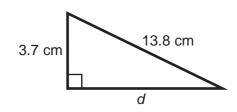
Pythagoras' Theorem

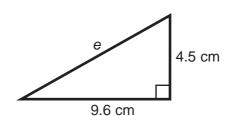
1) Calculate the lengths of the sides a to f, giving each answer to 1 decimal place.

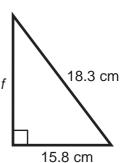




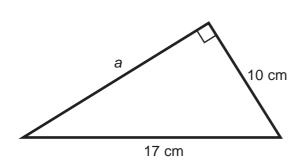


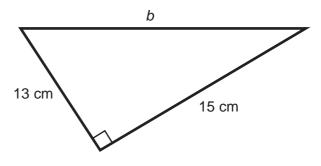




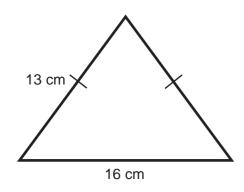


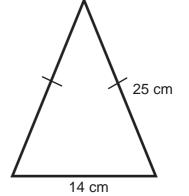
2) Calculate the lengths of the sides a and b, giving each answer to 1 decimal place.





- 3) Find the height of this isosceles triangle. Give your answer to 1 decimal place.
- 4) Find the area of this isosceles triangle.

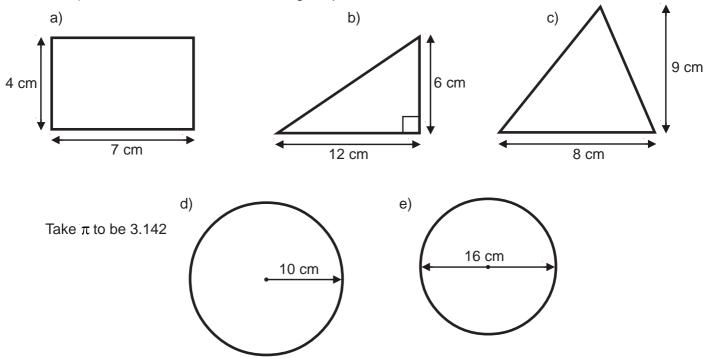




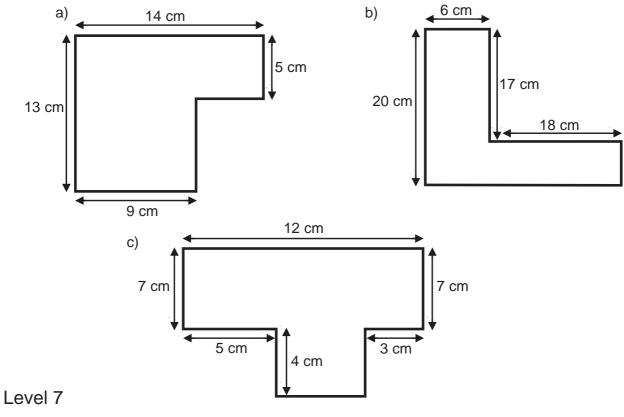
Level 7

Areas of Compound Shapes

Find the areas of the following shapes:



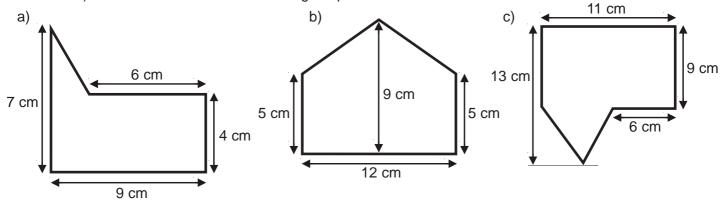
2) Find the areas of the following shapes:



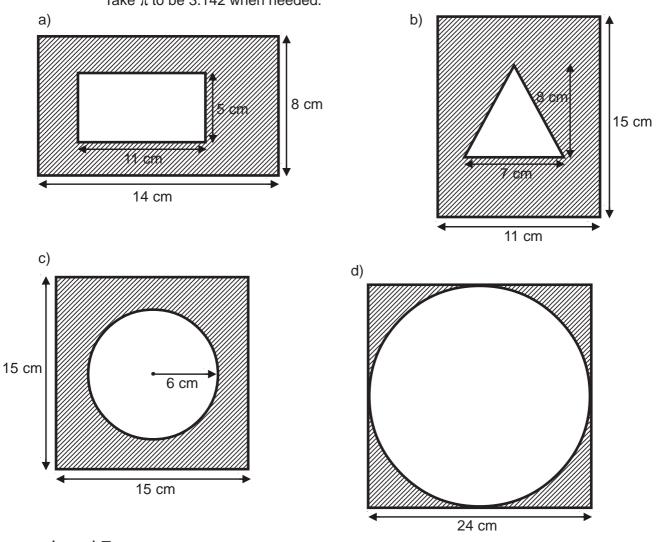
N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25

Areas of Compound Shapes

1) Find the areas of the following shapes:



2) Find the areas of the shaded parts of the following: Take π to be 3.142 when needed.

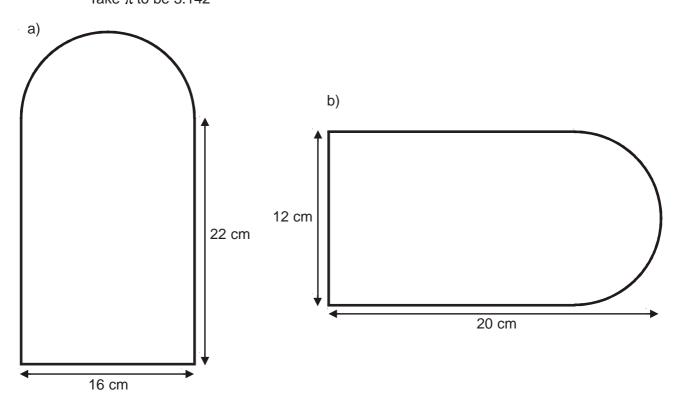


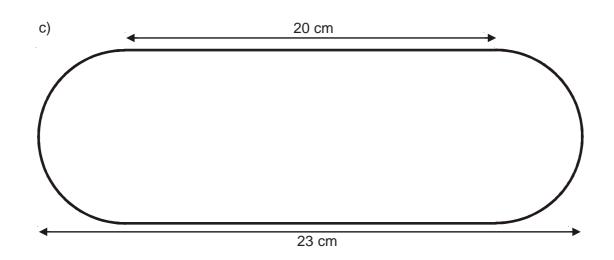
Level 7

N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25

Areas of Compound Shapes

Find the areas of the shapes below: Take π to be 3.142

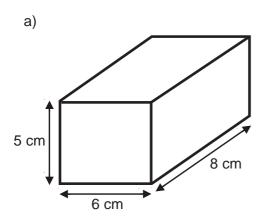


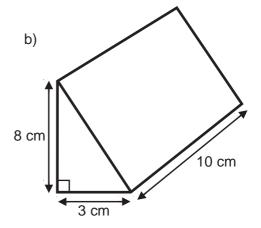


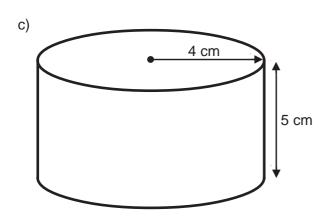
Level 7

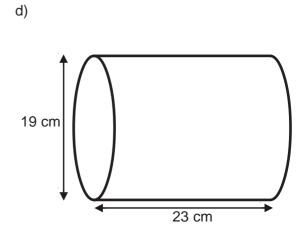
Volumes of Prisms

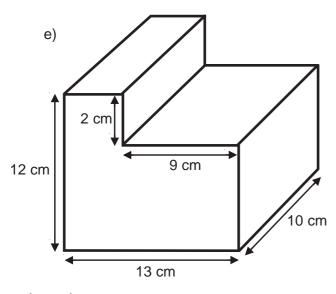
Find the volumes of the prisms, below. Take π to be 3.142 for questions c and d.

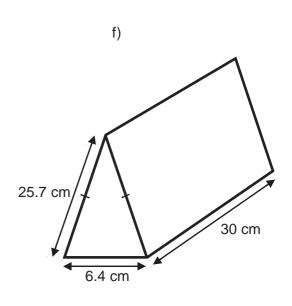












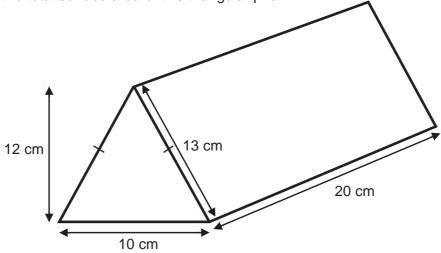
Level 7

N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 A26 A27 A28 A29 S30 S31 S\$2 S33 S34 S35 S36 S37 D14 D15

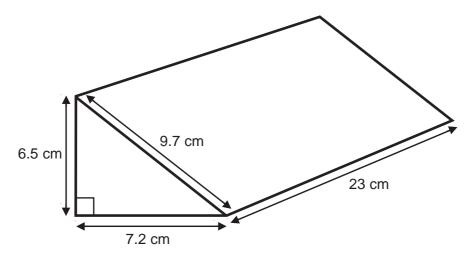
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Surface Area of Triangular Prisms

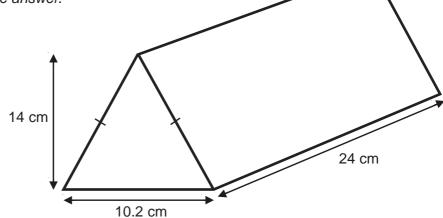
1) Find the total surface area of this triangular prism.



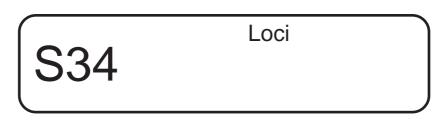
2) Find the total surface area of this triangular prism.



3) Find the total surface area of this triangular prism. You will need to use Pythagoras' theorem at some stage to get the answer.



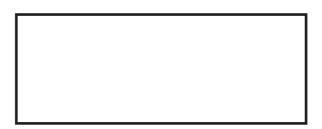
Level 7



1) Draw the locus of all the points that are 1.2 cm away from the line AB.



2) Draw the locus of all the points that are 1.5 cm away from the rectangle *ABCD*.



3) Radio signals can be heard within a 4.5 km radius of transmitter *A* and a 5.5 km radius of transmitter *B*. Show, by shading, the area where radio signals can be heard from both transmitters at the same time. *Use a scale of 1 cm represents 1 km*.



Level 7

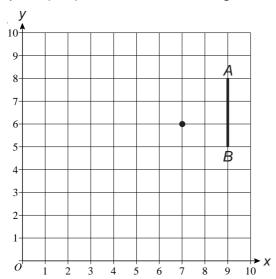
N22 C26 C27 C28 C29 C30 C31 A16 A17 A18 A19 A20 A21 A22 A23 A24 A25 A26 A27 A28 A29 S30 S31 S32 S33 S\$4 S35 S36 S37 D14 D15

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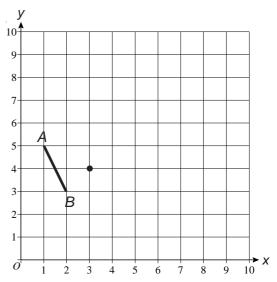
S35

Enlargement by a Negative Scale Factor

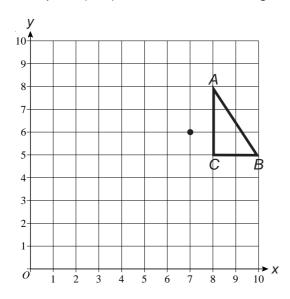
1) Enlarge line *AB* with scale factor -2 and point (7, 6) as the centre of enlargement.



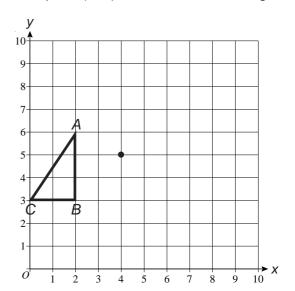
2) Enlarge line AB with scale factor -3 and point (3, 4) as the centre of enlargement.



3) Enlarge triangle *ABC* with scale factor -2 and point (7, 6) as the centre of enlargement.



4) Enlarge triangle *ABC* with scale factor -1.5 and point (4, 5) as the centre of enlargement.

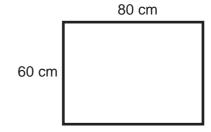


Level 7

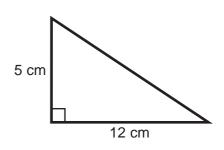
Bounds

S36

- 1) The length of a bracelet is 24 cm measured to the nearest centimetre.
 - Work out the lower bound of the length of the bracelet.
 - b) Work out the upper bound of the length of the bracelet.
- 2) The length of a snake is 80 cm measured to the nearest 10 centimetres.
 - a) Work out the lower bound of the length of the snake.
 - b) Work out the upper bound of the length of the snake.
- 3) The weight of a necklace is 145 g measured to the nearest 5 grams.
 - a) Work out the lower bound of the weight of the necklace.
 - b) Work out the upper bound of the weight of the necklace.
- 4) The length of a line is given as 17.2 cm measured to the nearest tenth of a centimetre.
 - a) Work out the lower bound of the length of the line.
 - b) Work out the upper bound of the length of the line.
- 5) A rectangle has a length of 80 cm and a width of 60 cm, both measured to the nearest 10 cm.
 - a) Work out the lower bound of the area of the rectangle.
 - b) Work out the upper bound of the perimeter of the rectangle.



- 6) A right-angled triangle has lengths as shown, all measured to the nearest centimetre.
 - a) Work out the lower bound of the area of the triangle.
 - b) Work out the upper bound of the area of the triangle.



Level 7

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Compound Measures

S37

- 1) A car travels at 60 mph for 3 hours. How far does the car travel?
- 2) A cyclist cycles for 4 hours and covers a distance of 48 miles. What was her average speed in miles per hour?
- 3) How long would it take a train which travels at an average speed of 80 mph to cover a distance of 400 miles?
- 4) A runner runs at a speed of 12 km/h for 3 hours and 15 minutes. How far does he run?
- 5) An aeroplane flies at an average speed of 510 mph. How long would it take to fly a distance of 2720 miles?
- 6) If a worm travels a distance of 8.25 m in 2 hours and 45 minutes, work out his average speed in metres per hour.
- 7) 12.5 cm³ of mercury has a mass of 170 g. Work out the density of mercury.
- 8) Platinum has a density of 21.4 g/cm³. What is the mass of 35 cm³ of platinum?
- 9) A quantity of ice had a mass of 62.56 g. Knowing that ice has a density of 0.92 g/cm³, work out how much ice there was, in cm³.
- 10) 15000 cm³ of nitrogen has a mass of 18.765 g. Work out the density of nitrogen in g/cm³.
- 11) 15000 cm³ of gold has a mass of 289.5 **kg**. Work out the density of gold in **g**/cm³.

Level 7

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Averages from Tables

D14

 Sally conducted a survey to see how many sandwiches each pupil brought to school in her class per day.
 The results can be seen in the table.

No. of sandwiches	Frequency
0	1
1	5
2	6
3	12
4	2

- a) What is the modal number of sandwiches brought to school?
- b) What is the median number of sandwiches brought to school?
- c) Work out the mean number of sandwiches brought to school. Give your answer to 1 decimal place.
- 2) 50 hippos were captured over the course of a year and weighed. The results can be seen in the table, below.

Weight of hippo in tonnes	Frequency
1.4 ≤ <i>w</i> < 1.7	5
$1.7 \le w < 2.0$	9
$2.0 \le w < 2.3$	15
2.3 ≤ w < 2.6	12
2.6 ≤ w < 2.9	7
$2.9 \le w < 3.2$	2

Work out an estimate for the mean weight of a hippo. Give your answer to 1 decimal place.

Level 7

Averages from Tables

D14

Jenny had a theory that if asked to guess the length of a line, children under the age of 10 would overestimate the length but adults would underestimate the length.

To help her decide if she was correct she asked 100 under-10s and 100 adults to guess the length of a 34 cm line.

The results can be seen in the two tables, below.

Children under the age of 10 estimates

Estimate of length in cm	Frequency
20 ≤ <i>l</i> < 24	4
24 ≤ <i>l</i> < 28	11
28 ≤ <i>l</i> < 32	24
32 ≤ / < 36	39
36 ≤ / < 40	22

Adult estimates

Estimate of length in cm	Frequency
20 ≤ <i>l</i> < 24	2
24 ≤ <i>l</i> < 28	6
28 ≤ <i>l</i> < 32	16
32 ≤ / < 36	62
36 ≤ / < 40	14

Use the results in the tables to see if Jenny was correct. Show all your workings.

Level 7

Relative Frequency

D15

 Peter bought an unfair dice from a Joke Shop.
 He didn't know how the dice was biased and so he rolled it 100 times and noted down which numbers came up.

He found that the number 6 occurred 8 times.

- a) What is the relative frequency of getting a six?
- b) If Peter rolls the dice 400 times, estimate how many 6s he will roll.
- 2) Mary had a bag containing four different colour marbles. She chose a marble, noted its colour and then replaced it, 80 times.

The results can be seen in this table.

Colour	No. of times chosen
Red	12
Blue	24
Green	18
Yellow	26

- a) Estimate the probability that a blue marble will be chosen on the next pick.
- b) If a marble is chosen and replaced 280 times, estimate how many times you would expect to choose a red marble.
- 3) Benford's law says that if you look at real-life sources of data (heights of mountains, populations of countries, etc) the number 1 will be the first digit with relative frequency 0.3 If you go through any newspaper and write down the first 20 numbers you come across, about how many of the numbers would you expect to begin with a '1'.

Level 7

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